

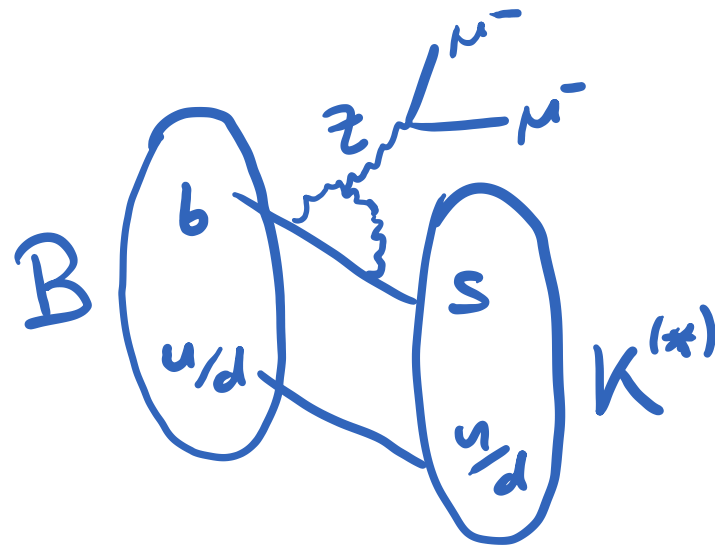
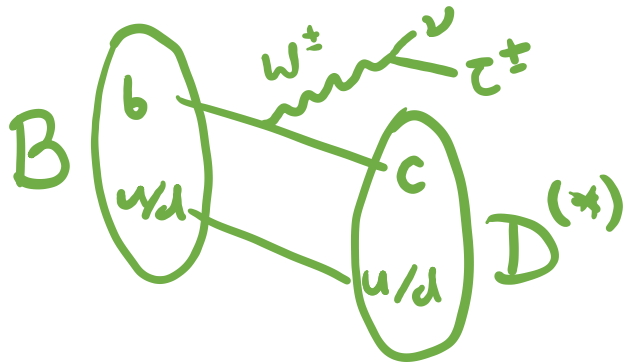
$B \rightarrow K^{(*)} \mu^+ \mu^-$ Anomalies at Future Colliders

Tevong You



What are the B anomalies?

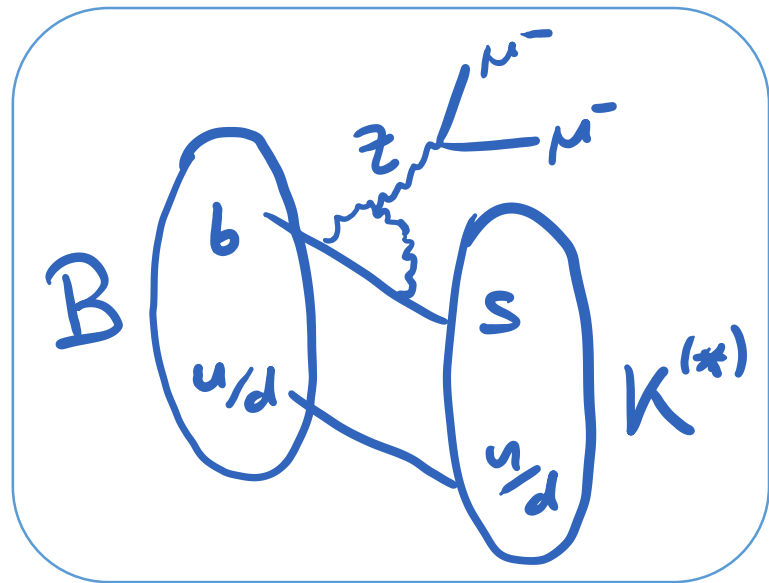
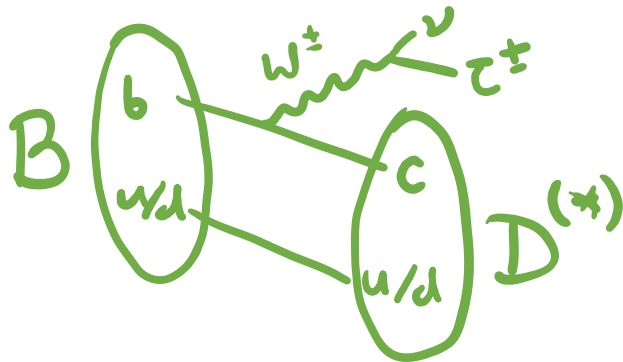
- Anomalies in **charged** ($B \rightarrow D^{(*)} \mu \nu$) and **neutral** ($B \rightarrow K^{(*)} \mu^+ \mu^-$) current B decays



- Focus on **neutral current** B decays

What are the B anomalies?

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- Focus on **neutral current** B decays

What are the B anomalies?

- Anomalies in processes involving $b \rightarrow s \mu^+ \mu^-$ transitions:

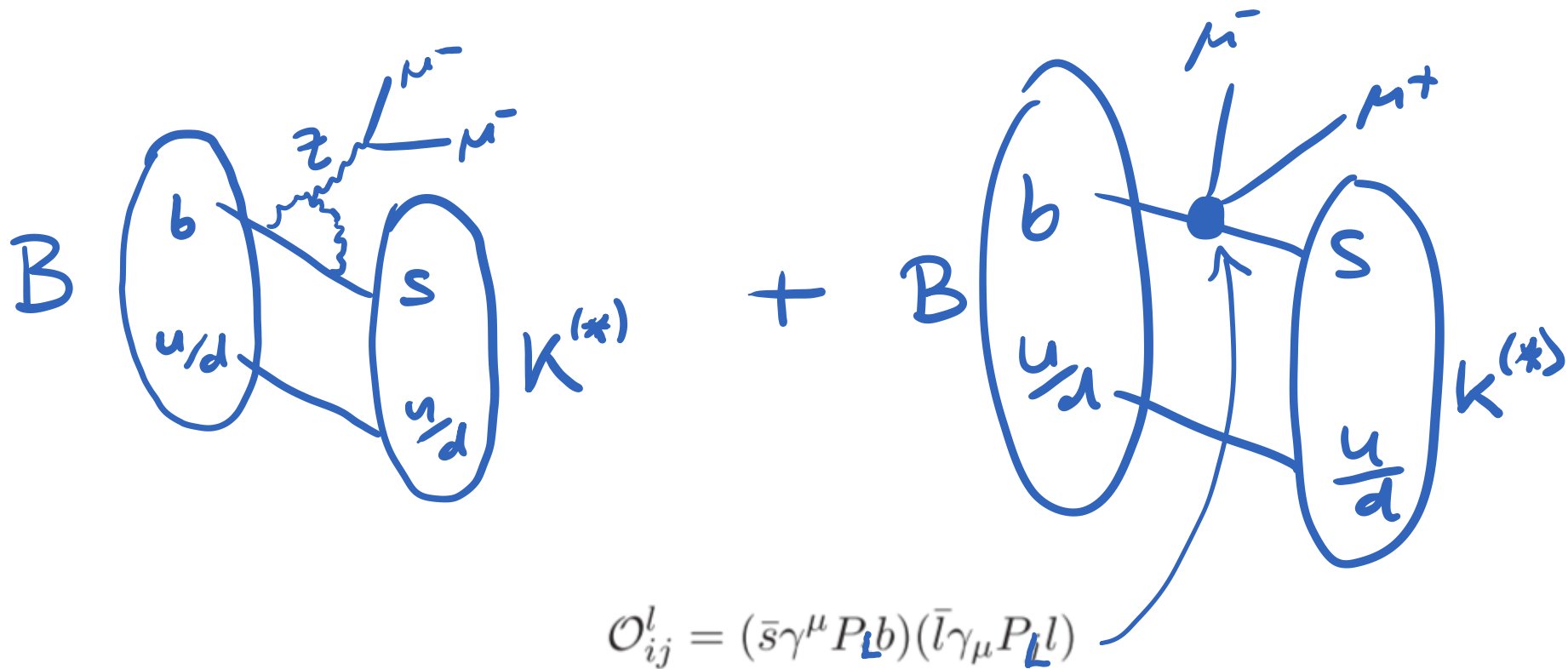
- LHCb **3.4 σ** in **P5'** angular distribution of $B \rightarrow K^* \mu^+ \mu^-$ (**2 σ** for Belle)
- Various **other kinematic observables** in $b \rightarrow s \mu^+ \mu^-$
- **3.2 σ** in $B_s \rightarrow \varphi \mu^+ \mu^-$
- $\Rightarrow$ **$\sim 4 \sigma$** non-zero Wilson coefficient in global fit to these “messy” observables

- **2.5 σ** in “clean” observable R_K
- **2.5 σ** in “clean” observable R_K^*
- $\Rightarrow$ **$\sim 4 \sigma$** non-zero Wilson coefficient in combined fit to just these two clean observables

- *Consistency* of all these various anomalies is **non-trivial**

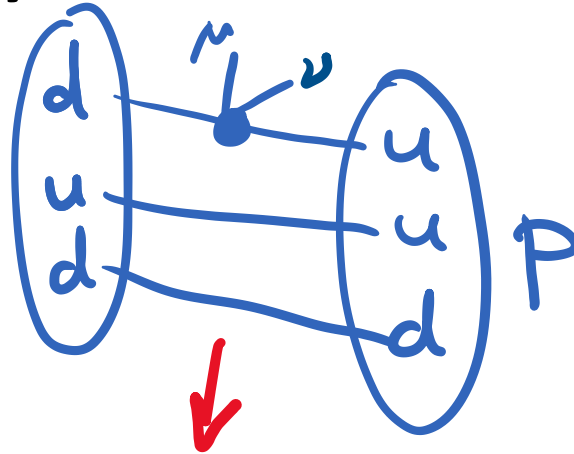
What are the B anomalies?

- Points towards **new physics** parametrised by a **four-fermion effective operator**

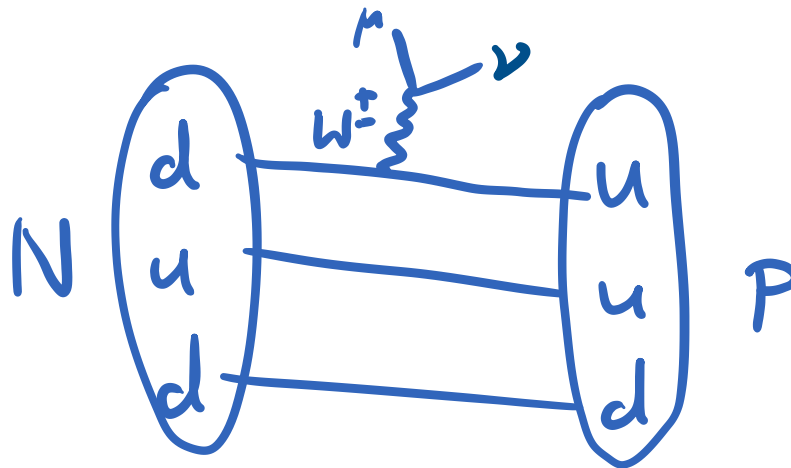


Historical Aside

- **Fermi theory** of radioactive beta decay:

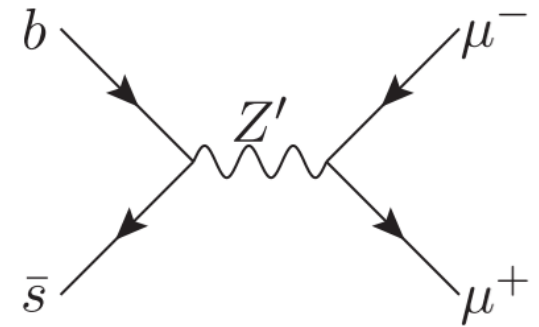
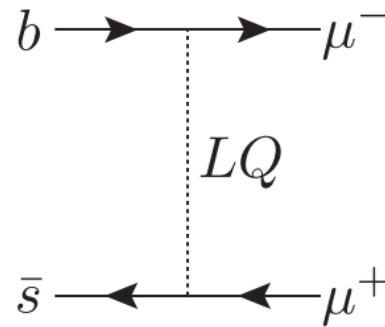
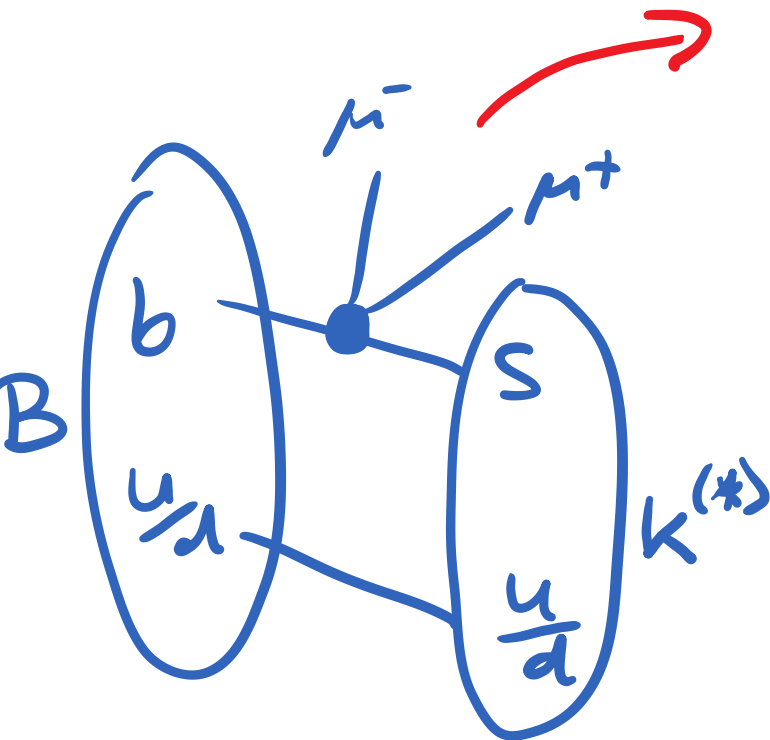


- Underlying new physics $\Rightarrow$ **electroweak gauge bosons**



New physics behind B anomalies?

- Z' or leptoquarks (at tree-level)



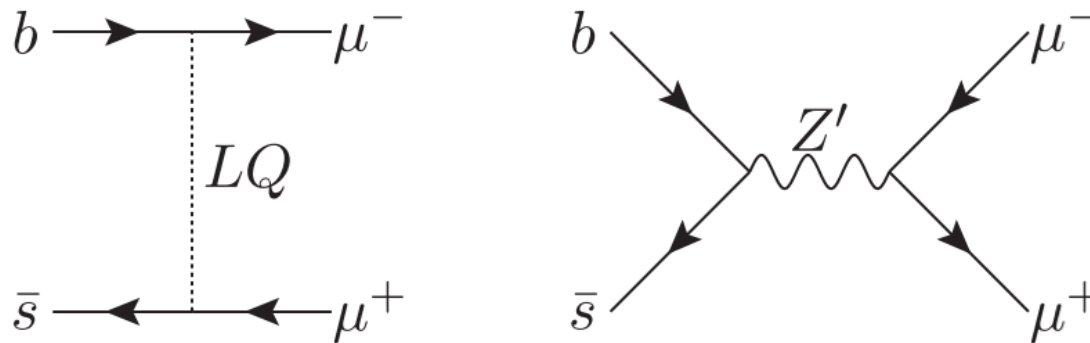
- What are the prospects for **exploring directly** this new sector?

Motivation for future colliders

- Can we *definitely* discover directly the source of the anomalies at higher energies?

80 TeV unitarity limit = **no general no-lose theorem** at FCC-hh (Di Luzio, Nardecchia [1706.01868])

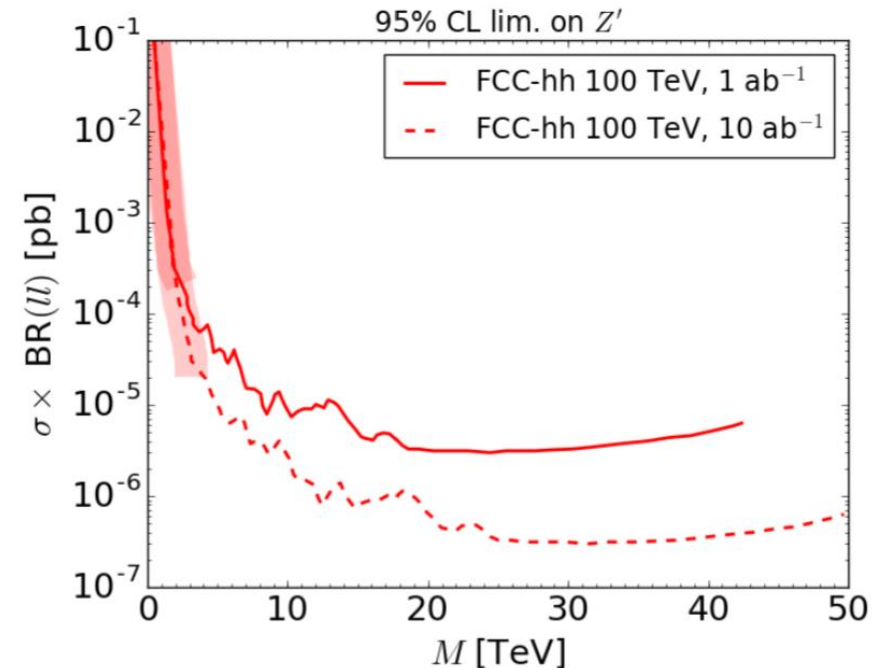
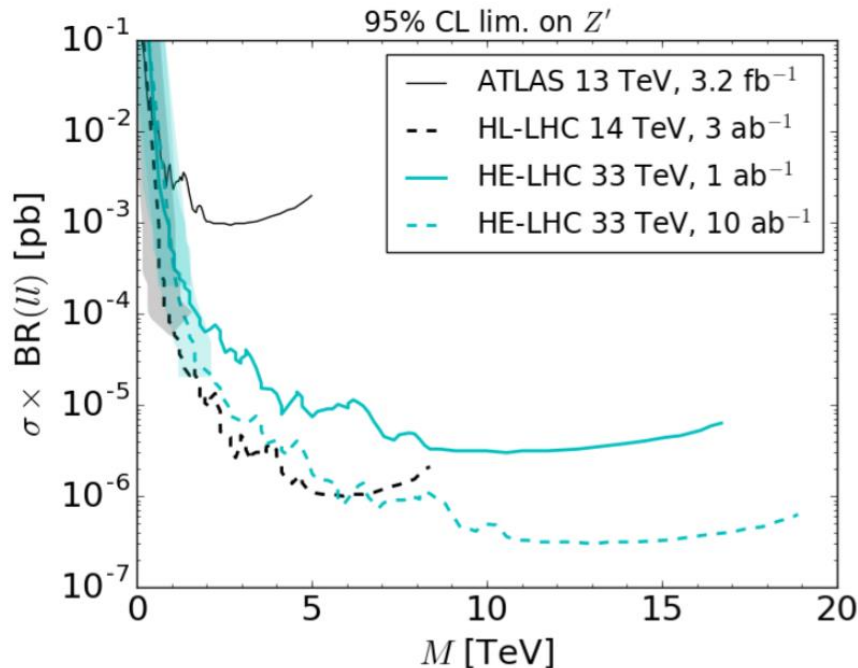
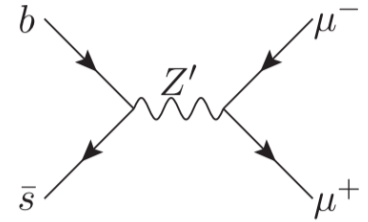
- Consider sensitivity to most **pessimistic** scenario: only include **minimal couplings** required to explain $b \rightarrow s\mu^+\mu^-$ anomalies



- More realistic models will typically be *easier* to discover

Z' Sensitivity

- Extrapolate current 13 TeV di-muon search:

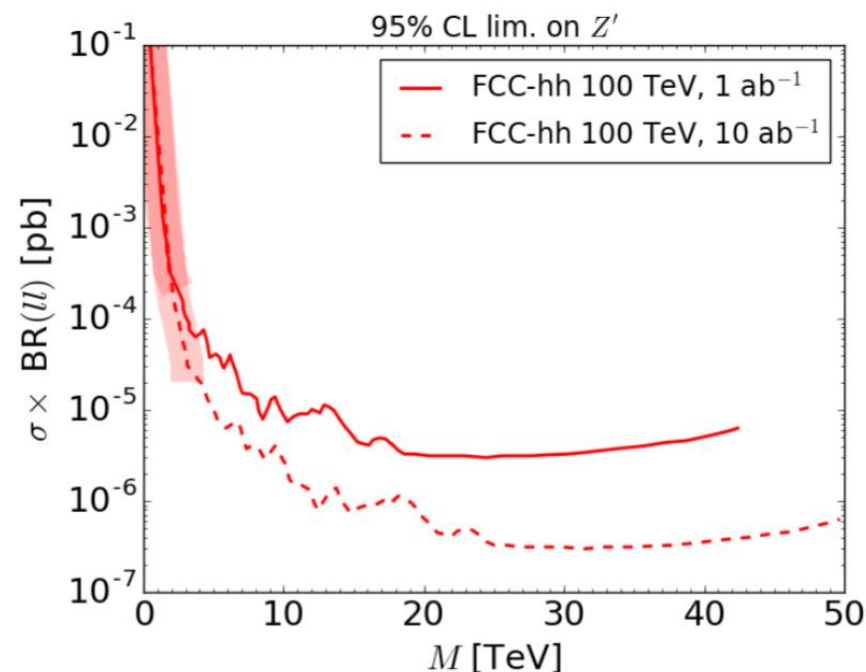
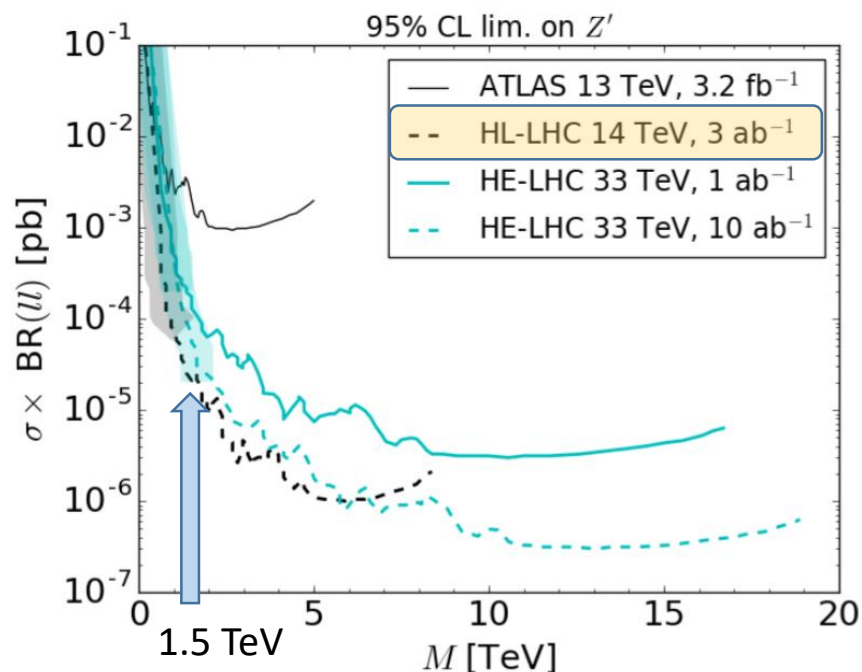
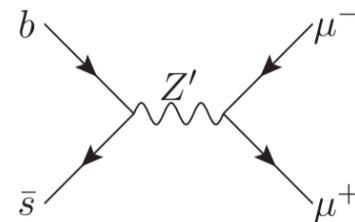


Allanach, Gripaos, TY [1710.06363]

- Actual limits depend on Z' couplings in signal x-section

Z' Sensitivity

- Extrapolate current 13 TeV di-muon search:

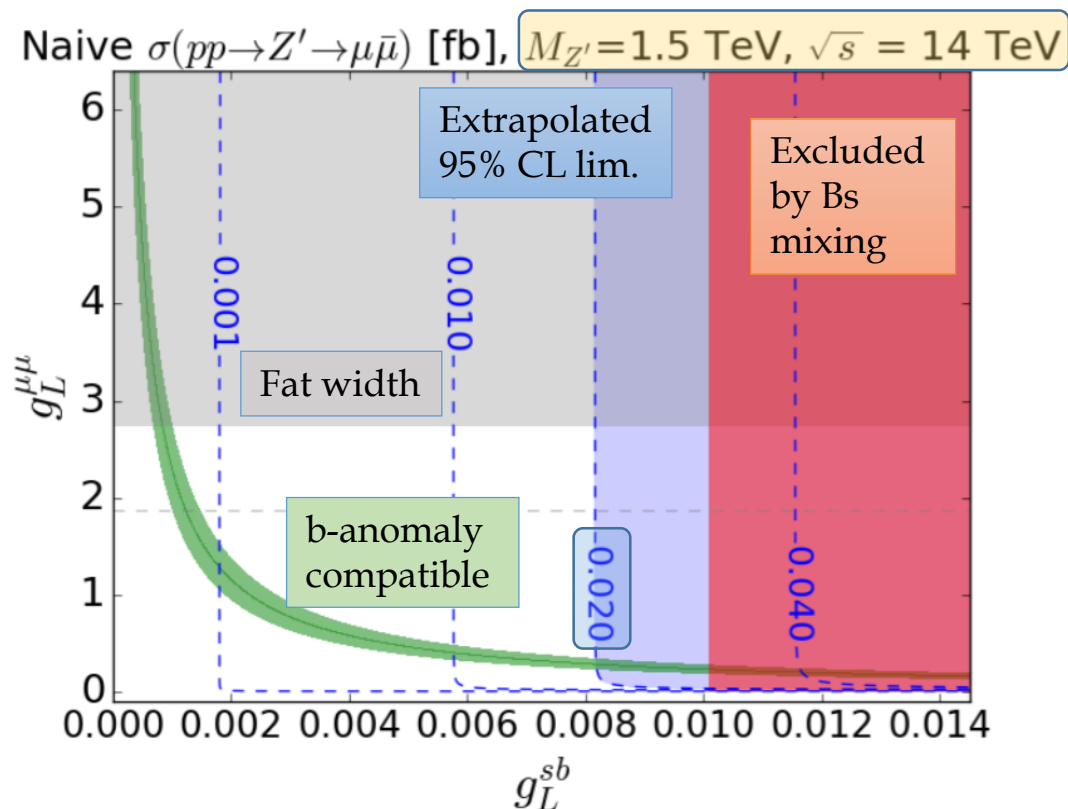
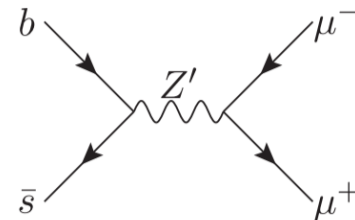


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Z' Sensitivity

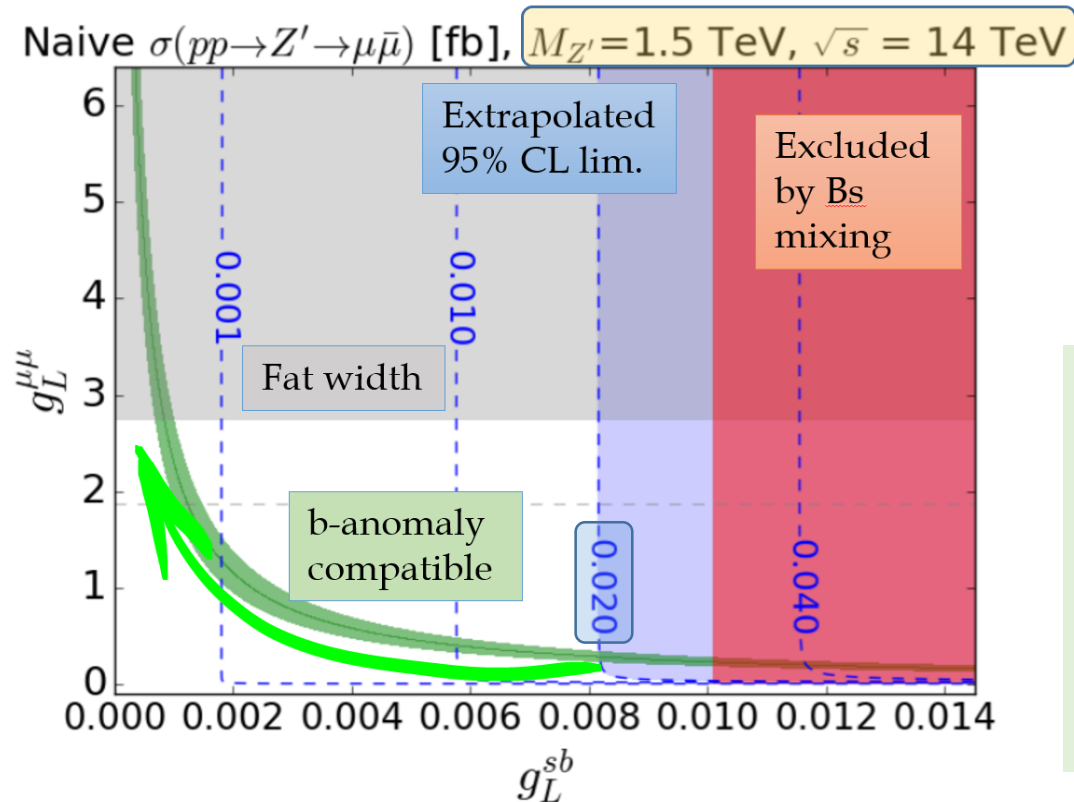
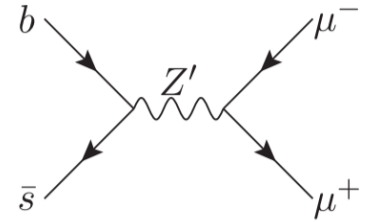
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Z' Sensitivity

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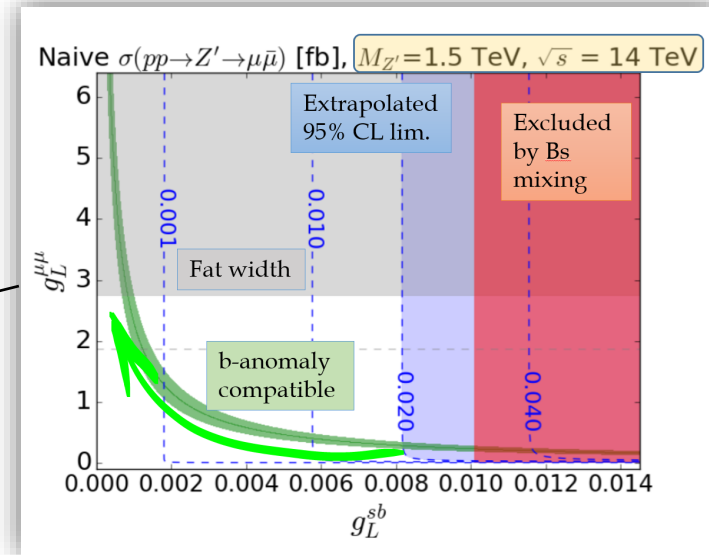
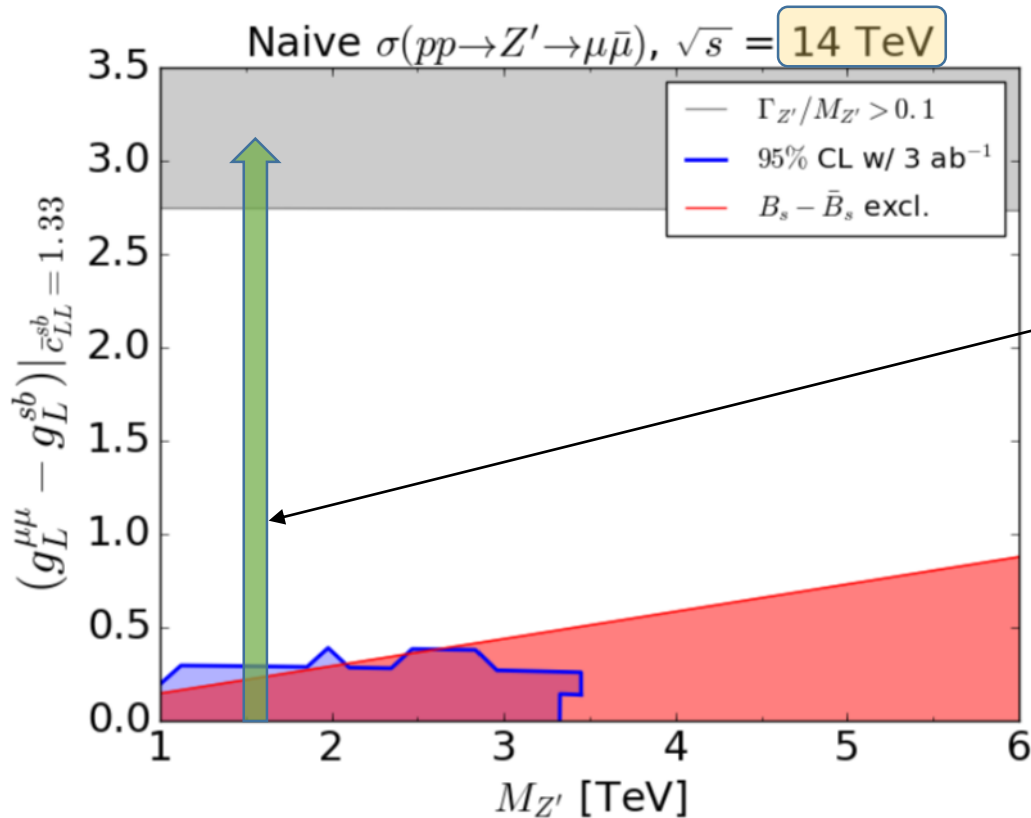
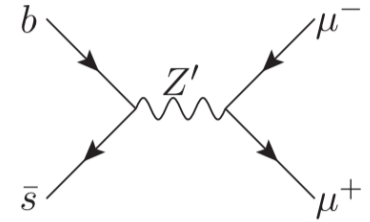


Summary of Z' coverage:
For each $M_{Z'}$, plot vertically the anomaly-compatible region

- Actual limits depend on Z' couplings in signal x-section

Z' Sensitivity

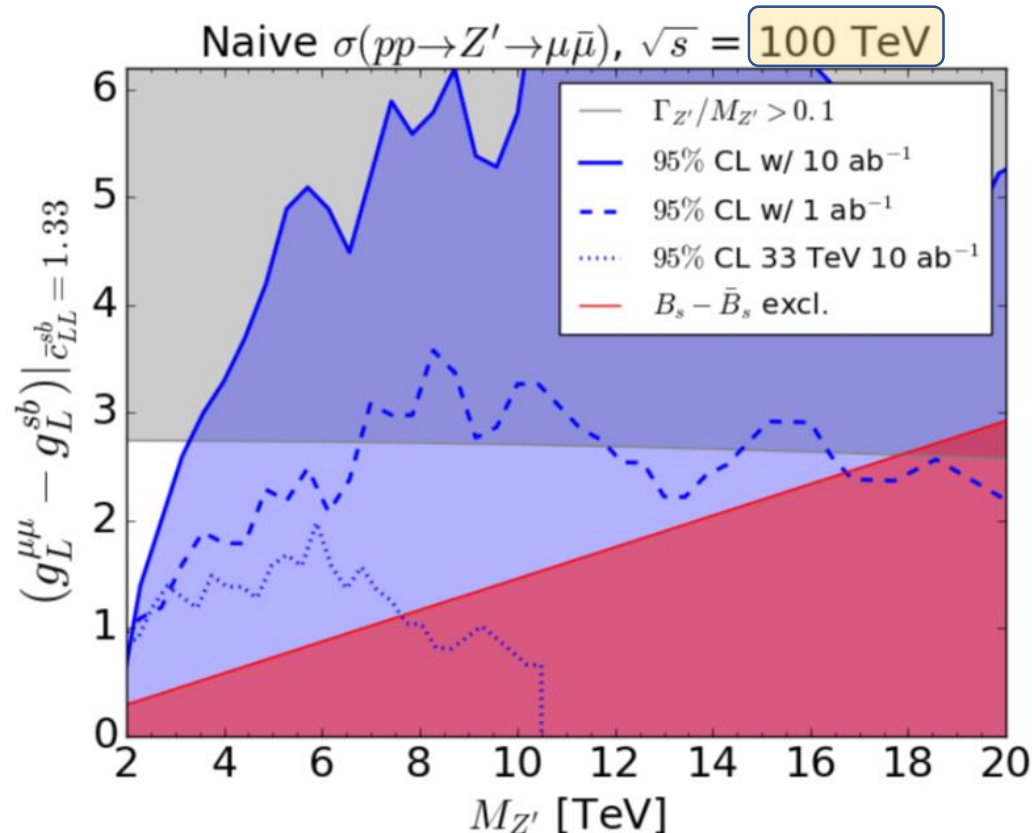
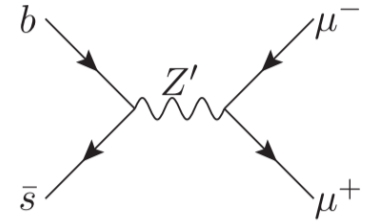
- Extrapolate current 13 TeV di-muon search:



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Z' Sensitivity

- Extrapolate current 13 TeV di-muon search:

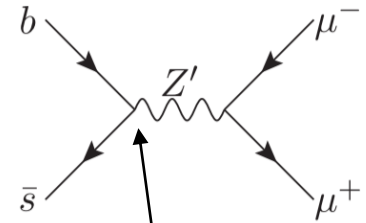
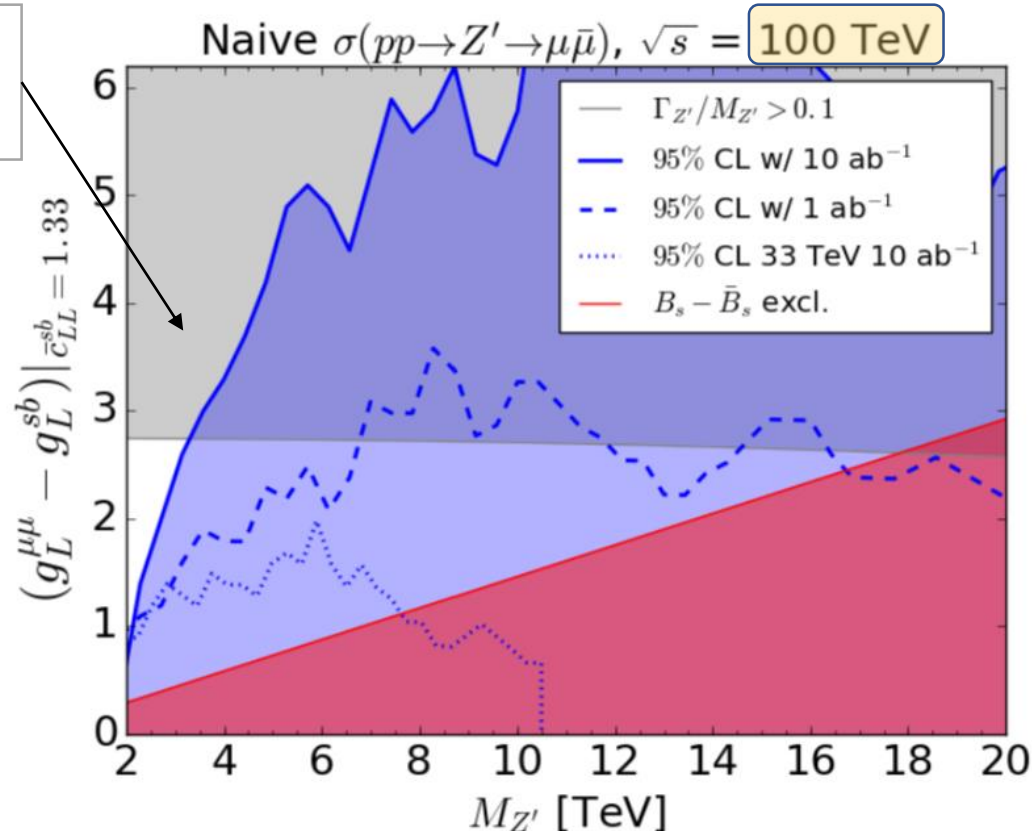


- 100 TeV can cover almost **all** (narrow width) parameter space of most *pessimistic* scenario

Z' Sensitivity

- Extrapolate current 13 TeV di-muon search:

Narrow width approximation no longer valid!



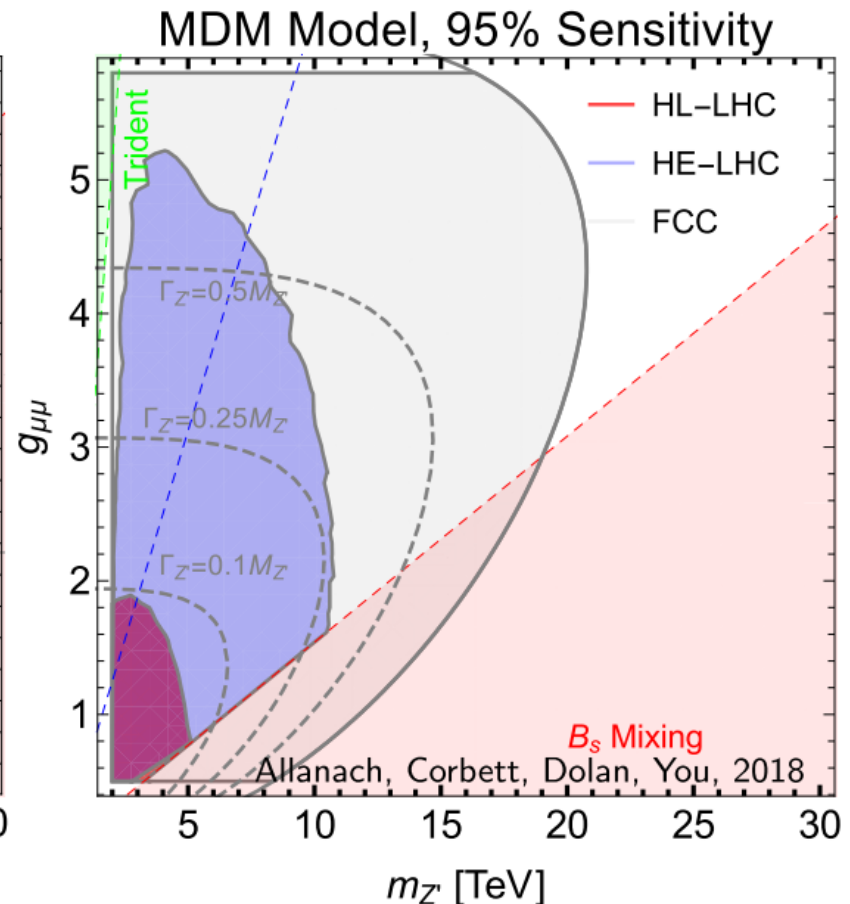
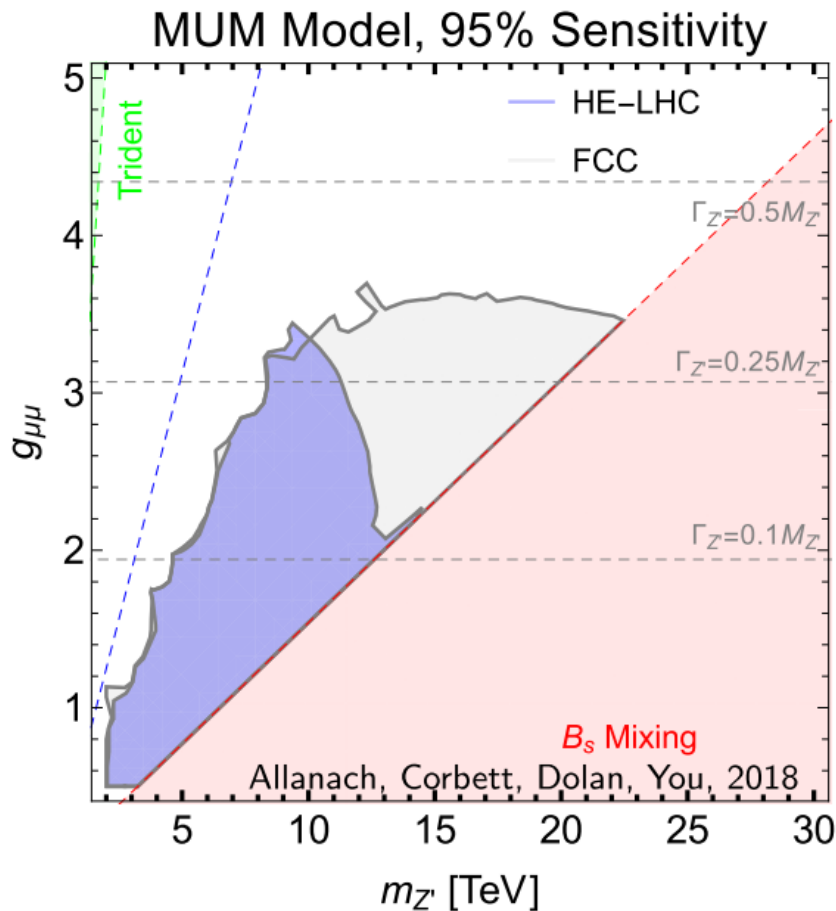
Necessarily have additional flavour structure...

- 100 TeV can cover almost **all** (narrow width) parameter space of most *pessimistic* scenario

Z' Sensitivity

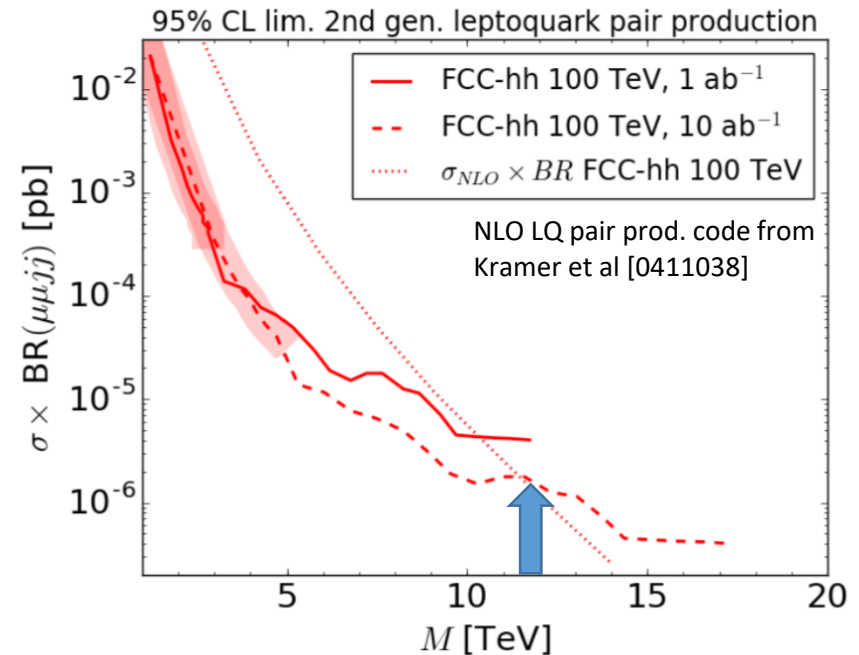
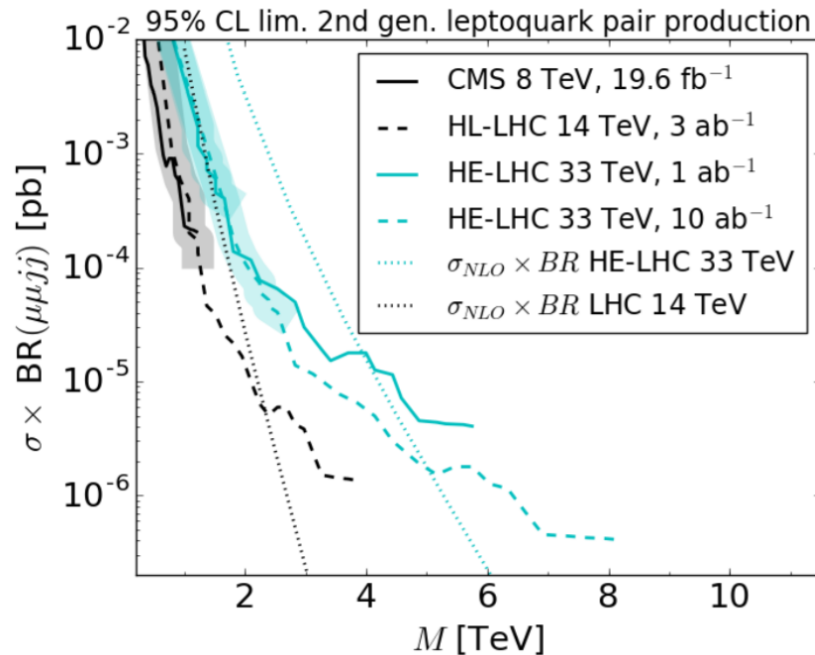
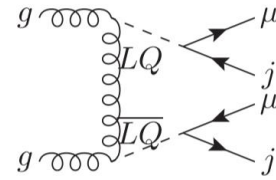
Allanach, Corbett, Dolan, TY [1810.02166]

- Improved MC study including **large widths** and **two benchmark flavour scenarios**:



Leptoquark Sensitivity

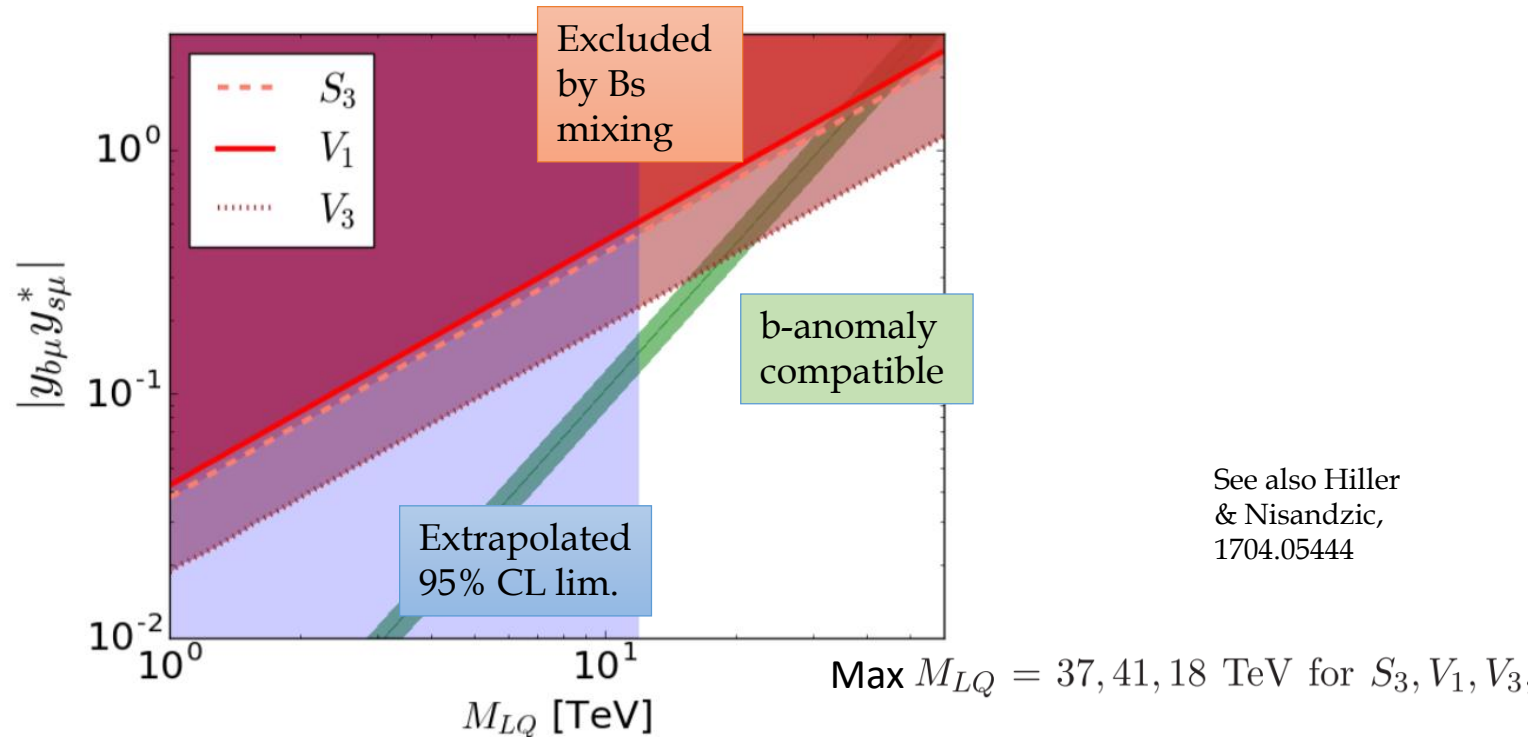
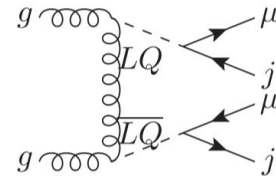
- Extrapolate current 8 TeV LQ di-muon+di-jet search:



- Pair production for scalar LQ depends only on QCD coupling
- Upper limit from B_s mixing constraint

Leptoquark Sensitivity

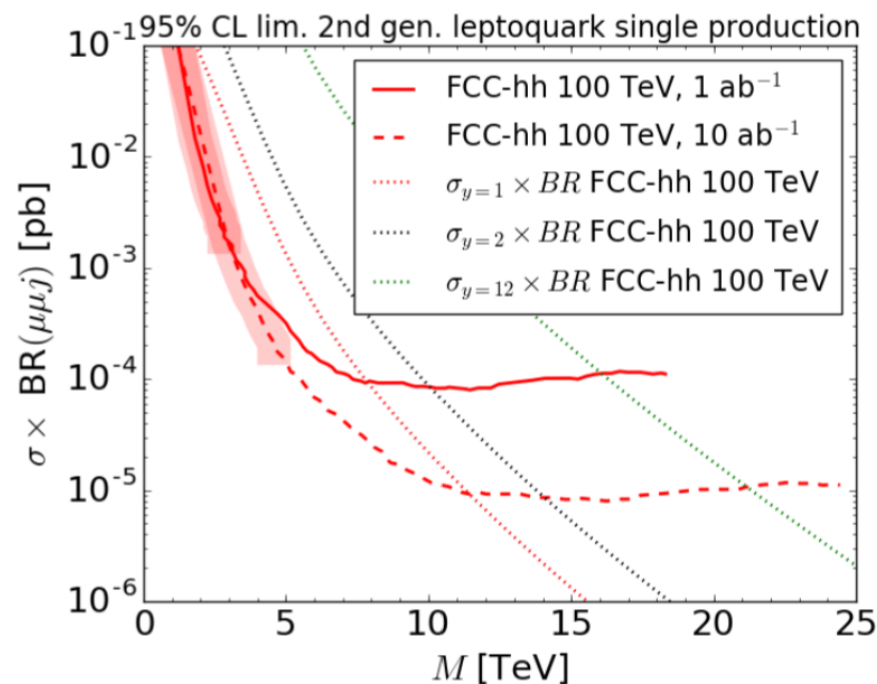
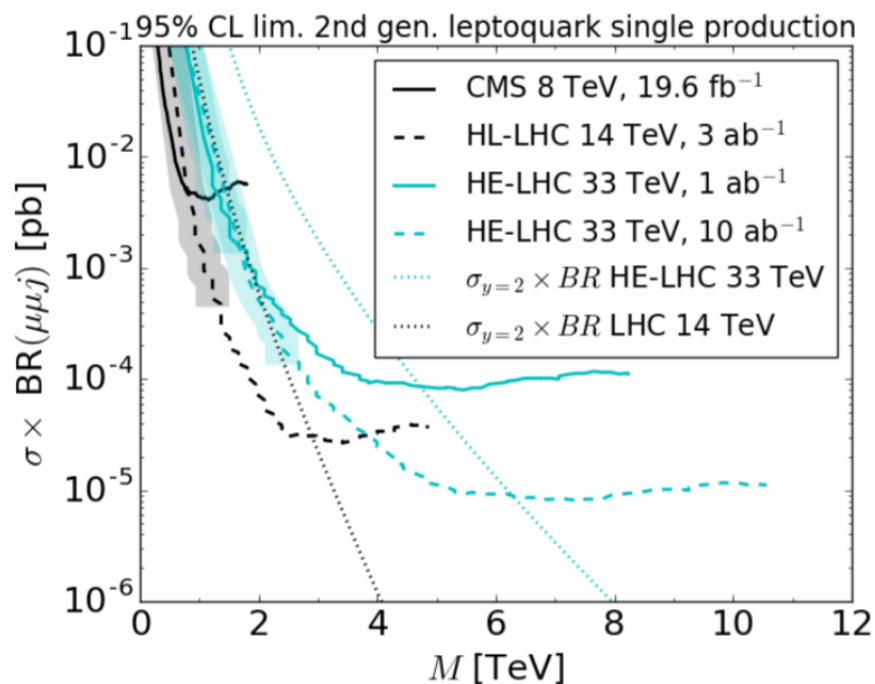
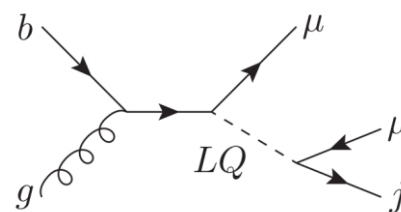
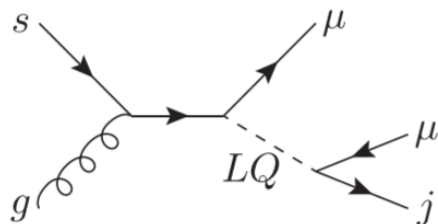
- Extrapolate current 8 TeV LQ di-muon+di-jet search:



See also Hiller
& Nisandzic,
1704.05444

- Pair production for scalar LQ depends only on QCD coupling
- Upper limit from B_s mixing constraint

Leptoquark single production



Conclusion

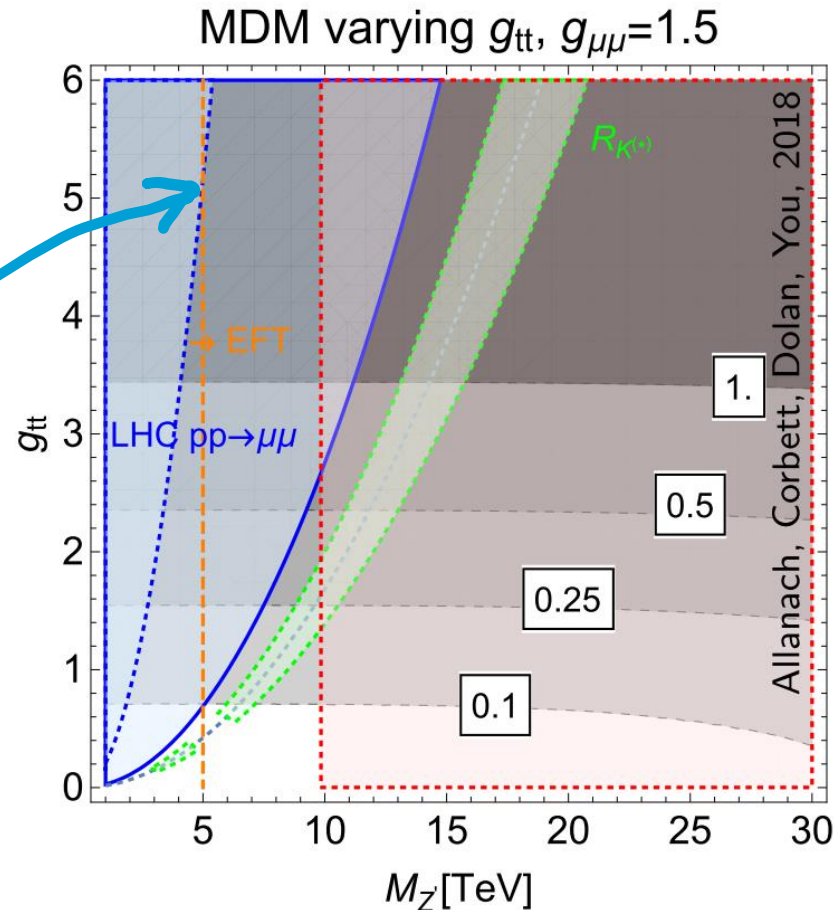
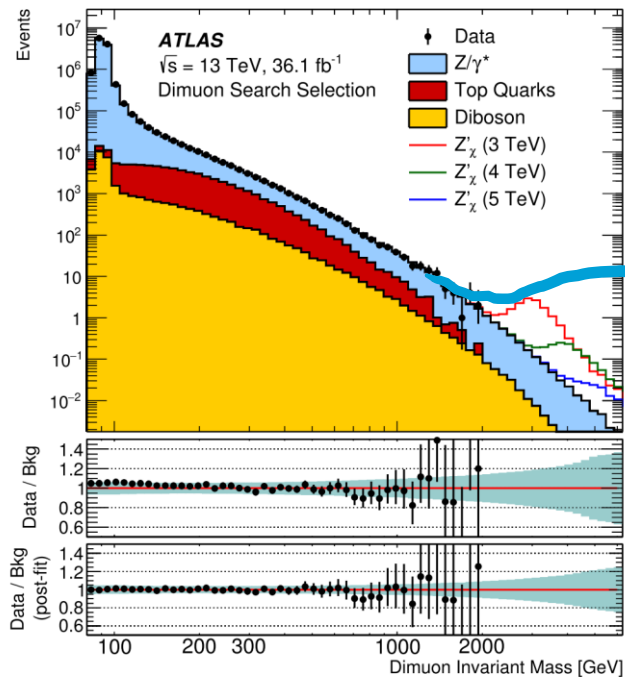
- If confirmed by LHCb Run 2 update *and* Belle II...
- **Accessible scale** of new physics
- **First studies** of direct search potential at future colliders
- **B anomalies could shed light on many BSM questions**
- Even if anomalies vanish, motivates interplay between **direct** discovery potential of future hadron colliders and **indirect** sensitivity from precision physics

Backup

Z' Sensitivity

Allanach, Corbett, Dolan, TY [1810.02166]

- **Indirect effects** from effective operators in LHC di-muon tail would point towards **fat Z'** at higher energies



$$\mathcal{L}_{Z'f} = \left(\overline{\mathbf{Q}'_{Li}} \lambda_{ij}^{(Q)} \gamma^\rho \mathbf{Q}'_{Lj} + \overline{\mathbf{L}'_{Li}} \lambda_{ij}^{(L)} \gamma^\rho \mathbf{L}'_{Lj} \right) Z'_\rho,$$



$$V = V_{u_L}^\dagger V_{d_L}, \quad U = V_{\nu_L}^\dagger V_{e_L}$$

$$\mathcal{L} = \left(\overline{\mathbf{u}_L} V \Lambda^{(Q)} V^\dagger \gamma^\rho \mathbf{u}_L + \overline{\mathbf{d}_L} \Lambda^{(Q)} \gamma^\rho \mathbf{d}_L + \overline{\mathbf{n}_L} U \Lambda^{(L)} U^\dagger \gamma^\rho \mathbf{n}_L + \overline{\mathbf{e}_L} \Lambda^{(L)} \gamma^\rho \mathbf{e}_L \right) Z'_\rho,$$

$$\Lambda^{(Q)} \equiv V_{d_L}^\dagger \lambda^{(Q)} V_{d_L}, \quad \Lambda^{(L)} \equiv V_{e_L}^\dagger \lambda^{(L)} V_{e_L}$$

The ‘mixed up-muon’ (MUM) model

$$\Lambda^{(Q)} = g_{bs} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \quad \Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

The ‘mixed down-muon’ (MDM) model

$$\Lambda^{(Q)} = g_{tt} V^\dagger \cdot \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot V, \quad \Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

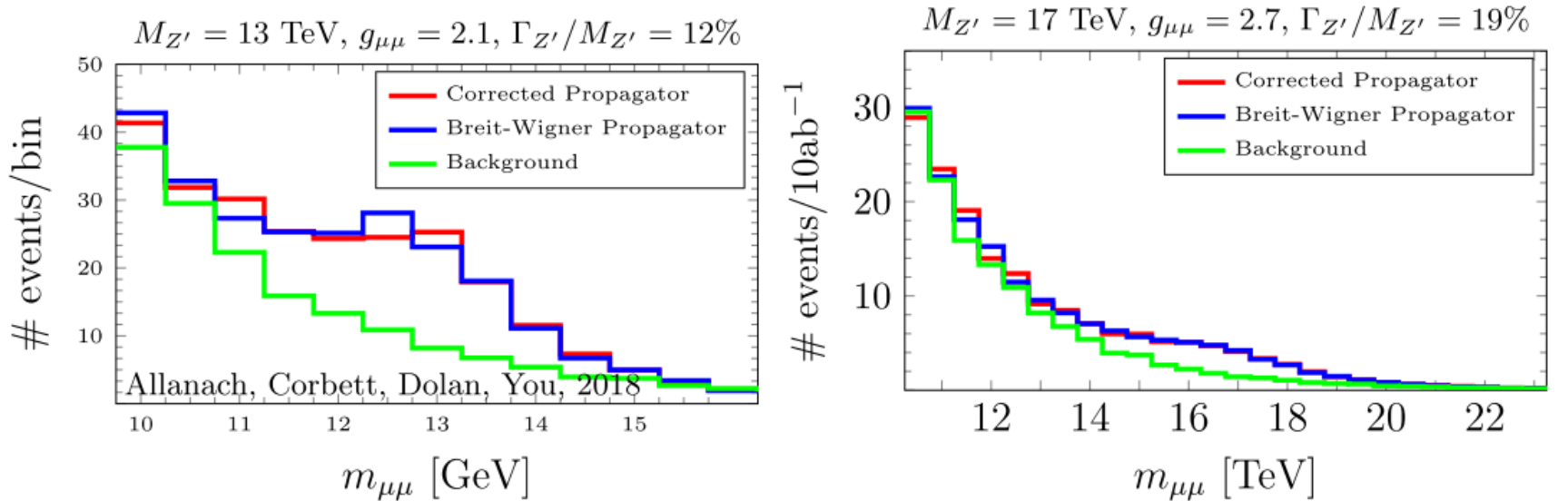


Figure 6. Expected di-muon invariant mass distributions at the FCC for (left) $M_{Z'}=13$ TeV, $g_{\mu\mu} = 2.1$ and (right) $M_{Z'}=17$ TeV, $g_{\mu\mu} = 2.7$, corresponding to widths of 12% and 19% respectively. The expected number of events per bin on the ordinate is for 10 ab^{-1} of integrated luminosity. This figure shows the difference between using the **MadGraph5** default propagator and the new propagator $\sim 1/(p^2 - M^2 - ip^2\Gamma/M)$. The significance for $M_{Z'} = 13$ TeV is 8.5 (9.7 for the default propagator) summing from bin 4 (5). The significance for $M_{Z'} = 17$ TeV is 4.6 (5.6) summing from bin 9 (10). All histograms and significance calculations are post-detector simulation (i.e. **DELPHES 3**).

$$M_{Z'} = 13 \text{ TeV}, g_{\mu\mu} = 2.1, \Gamma_{Z'}/M_{Z'} = 12\%$$

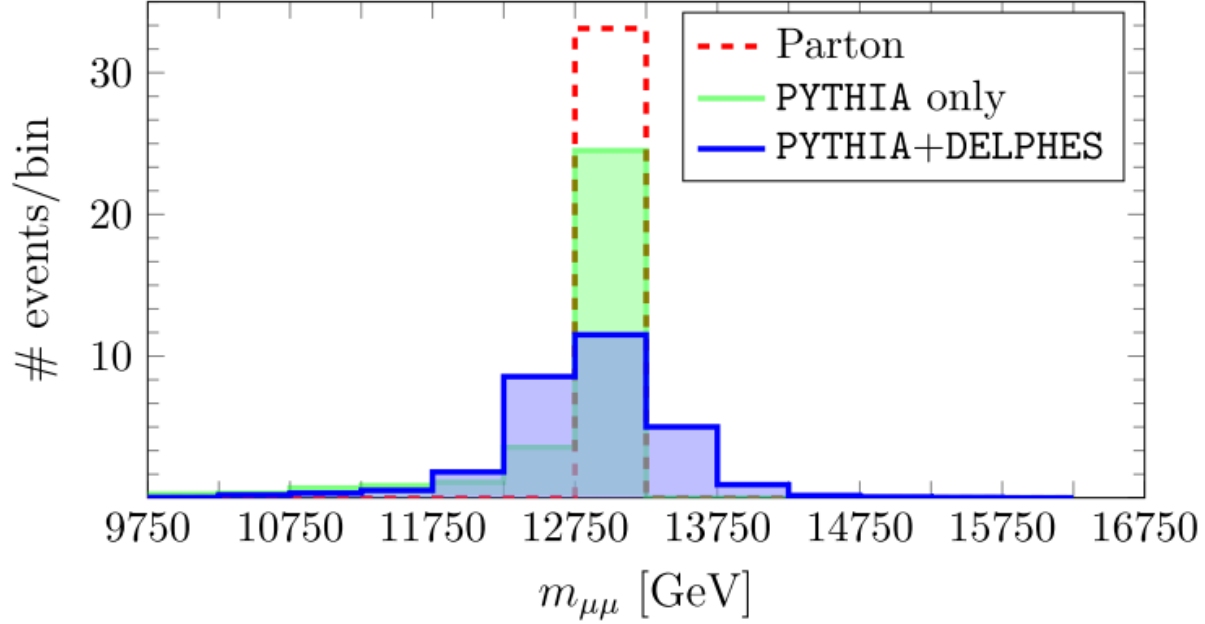


Figure 7. The bleeding of a single parton level bin centred on $m_{\mu\mu} = 13 \text{ TeV}$ for the Z' signal at the FCC. At parton-level, we expect 33.1 events (in 10 ab^{-1}), after parton showering effects are simulated by PYTHIA this reduces to 31.3 and after simulating detector effects with DELPHES 3, 29.2.

We define signal sensitivity as follows: first, we define a window of di-muon invariant mass in which to generate events, depending upon the collider:

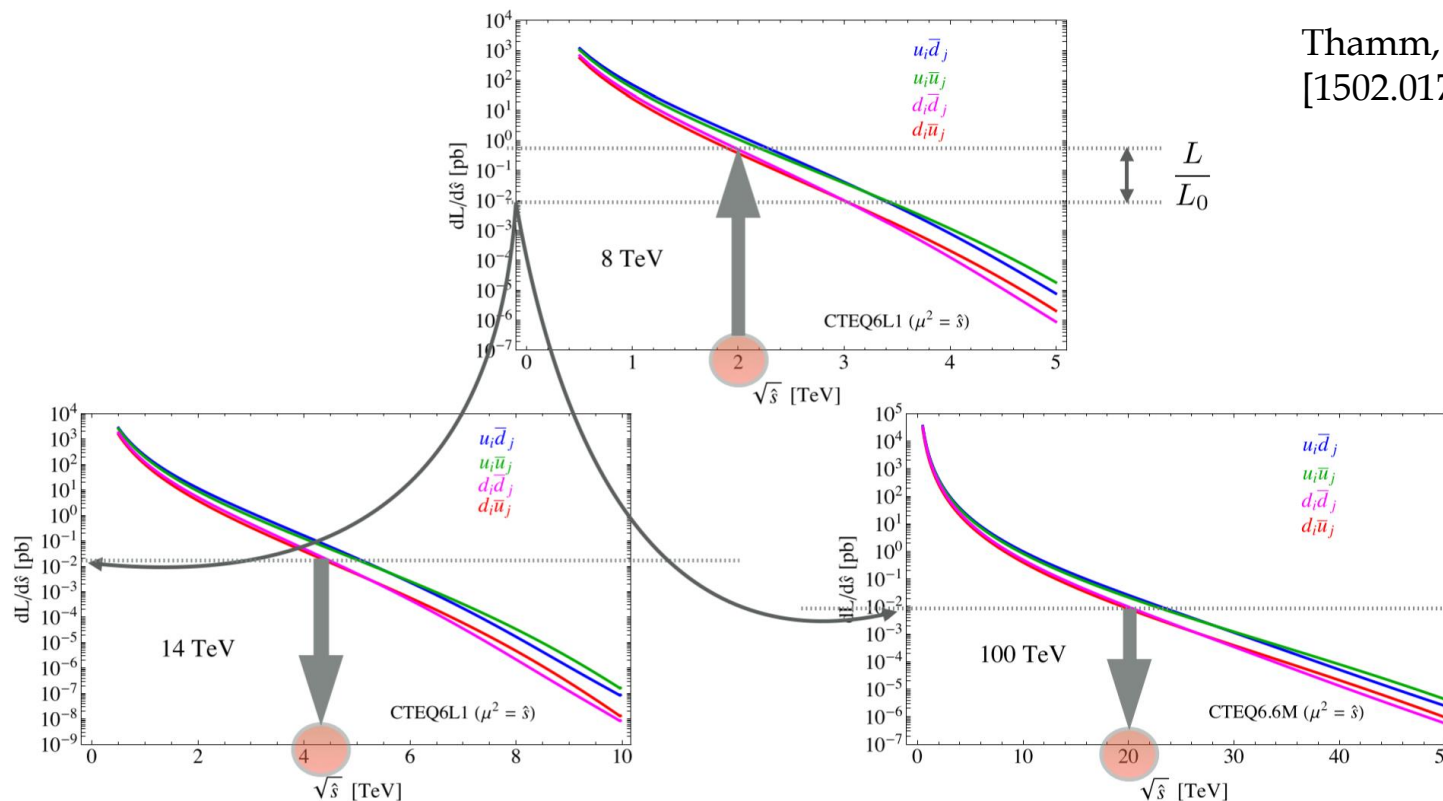
$$\begin{aligned} m_{\mu\mu}^{\text{HL-LHC}} &\in [\max\{M_{Z'} - \Gamma - 500 \text{ GeV}, 100 \text{ GeV}\}, \min\{M_{Z'} + \Gamma, 5.9 \text{ TeV}\}] \\ m_{\mu\mu}^{\text{HE-LHC}} &\in [\max\{M_{Z'} - \Gamma - 2 \text{ TeV}, 250 \text{ GeV}\}, \min\{M_{Z'} + \Gamma, 11.25 \text{ TeV}\}] \\ m_{\mu\mu}^{\text{FCC}} &\in [\max\{M_{Z'} - \Gamma - 2 \text{ TeV}, 250 \text{ GeV}\}, \min\{M_{Z'} + \Gamma, 25.25 \text{ TeV}\}]. \end{aligned}$$

We define $S_i \equiv (\sigma_i^{Z'+SM} - \sigma_i^{SM})\mathcal{L}$, where $\mathcal{L}$ is assumed integrated luminosity and $i \in \{1, \dots, N\}$, as the expected number of signal events in a single bin of width W in $m_{\mu\mu}$ estimated in our simulations⁸. $W = 500 \text{ GeV}$ is taken for all simulations apart from the HL-LHC ones, where $W = 100 \text{ GeV}$ is taken. $\sigma_i^{Z'+SM}$ is the $pp \rightarrow \mu^+\mu^-$ cross-section including the Z' lying in the $m_{\mu\mu}$ bin i and σ_i^{SM} is the SM $\mu^+\mu^-$ cross-section in the same bin⁹. Each of these cross-sections is to be understood as being for $pp \rightarrow \mu^+\mu^-$ after acceptance, efficiency and detector effects. The total significance, measured in terms of ‘number of σ ’, is defined to be

$$S = \max_i D_i, \quad \text{where} \quad D_i \equiv \frac{\sum_{j=i}^N S_j}{\sqrt{\sum_{k=i}^N B_k}}, \quad (3.3)$$

Extrapolation Method

- 95% CL limit depends on number of background events
- For current limit at given mass, find equivalent mass at future collider with same number of background = same limit at equivalent mass



Thamm, Torre, Wulzer
[1502.01701]

Extrapolation method

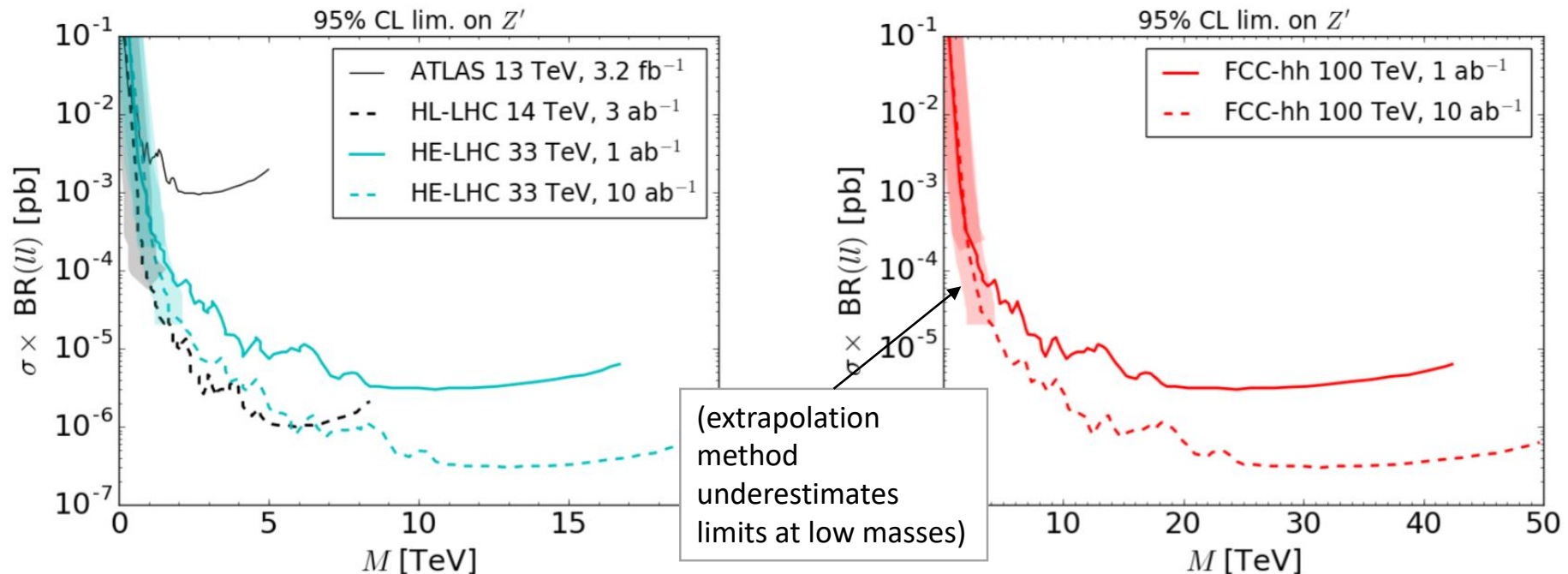
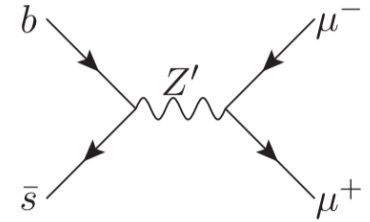
$$\sigma_B(M, s) \propto \sum_{i,j} \int_{M^2 - \Delta \hat{s}}^{M^2 + \Delta \hat{s}} d\hat{s} \frac{dL_{ij}}{d\hat{s}} \hat{\sigma}_{ij}(\hat{s}), \quad C_{ij} = \hat{s} \hat{\sigma}_{ij} \text{ is approximately constant.}$$

$$\propto \frac{\Delta \hat{s}}{M^2} \sum_{i,j} C_{ij} \frac{dL_{ij}}{d\hat{s}}(M, s)$$

$$L_0 \cdot \sum_{i,j} C_{ij} \frac{dL_{ij}}{d\hat{s}}(M_0, s_0) = L' \cdot \sum_{i,j} C_{ij} \frac{dL_{ij}}{d\hat{s}}(M', s')$$

Z' Sensitivity

- Extrapolate current 13 TeV di-muon search:

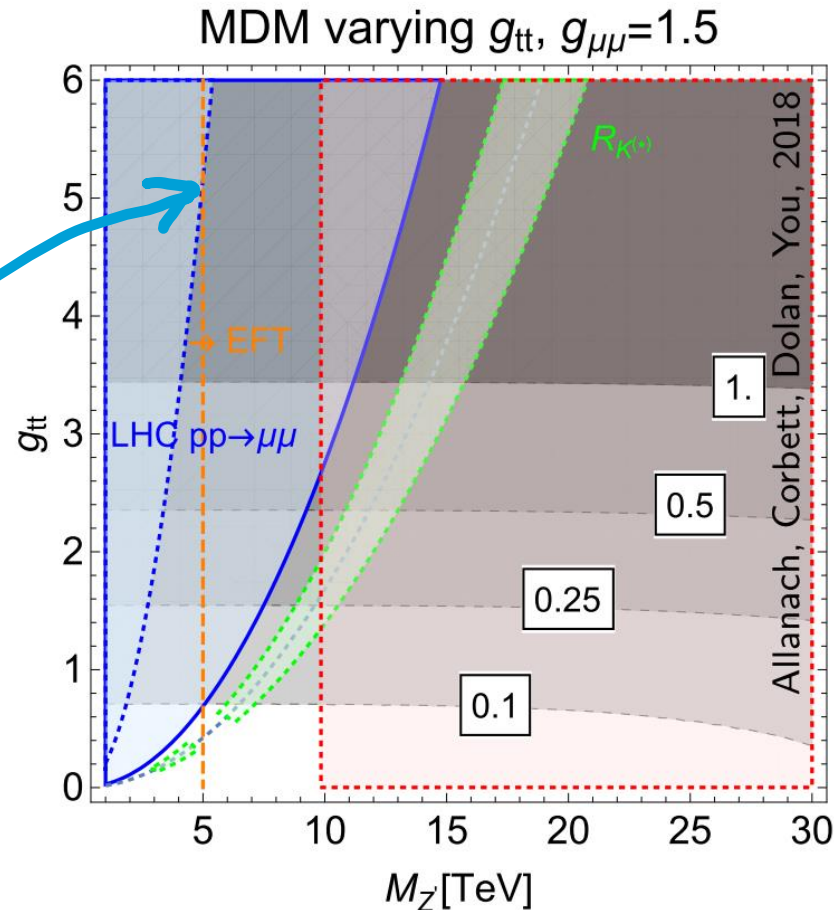
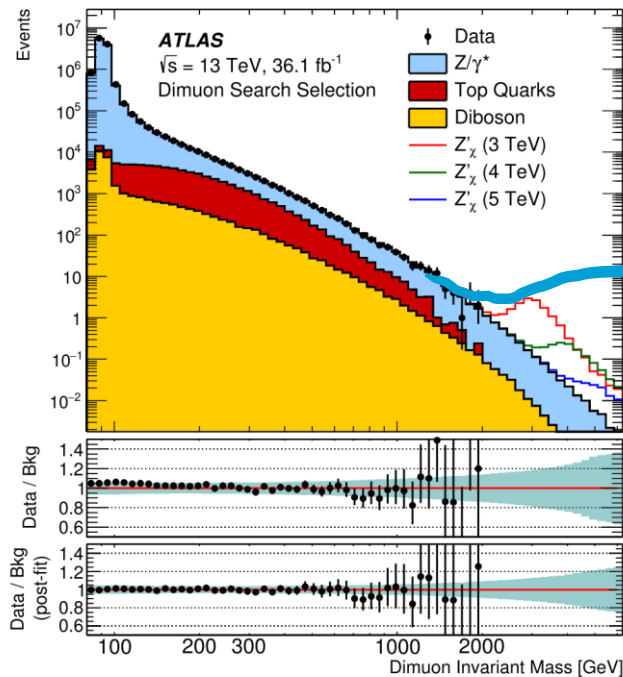


- Actual limits depend on Z' couplings in signal x-section

Z' Sensitivity

Allanach, Corbett, Dolan, TY [1810.02166]

- **Indirect effects** from effective operators in LHC di-muon tail would point towards **fat Z'** at higher energies

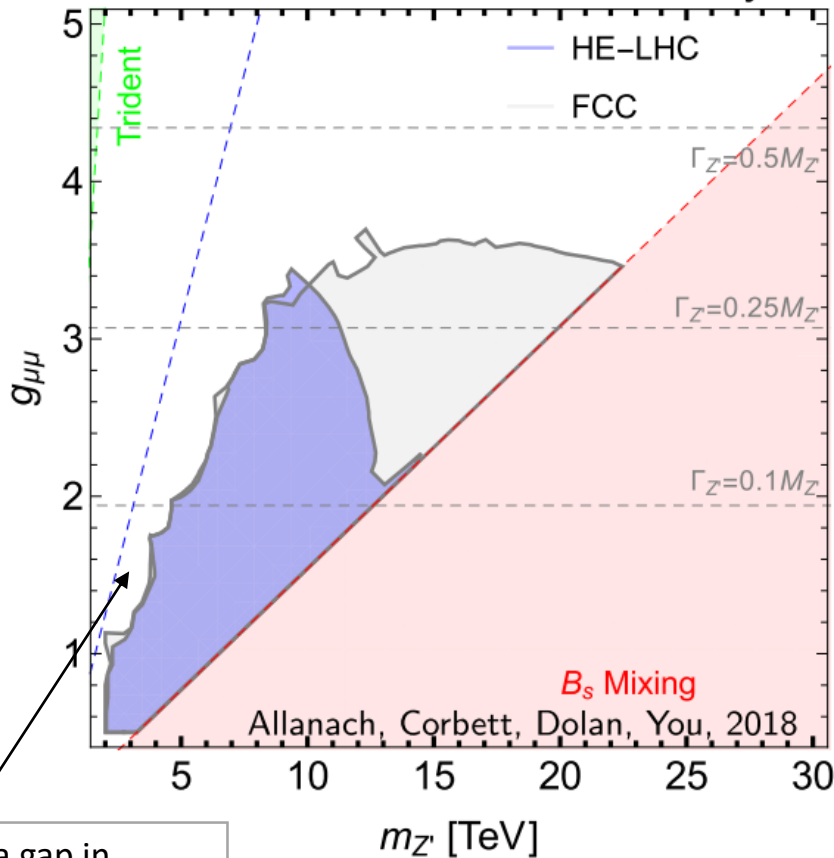


Z' Sensitivity

Allanach, Corbett, Dolan, TY [1810.02166]

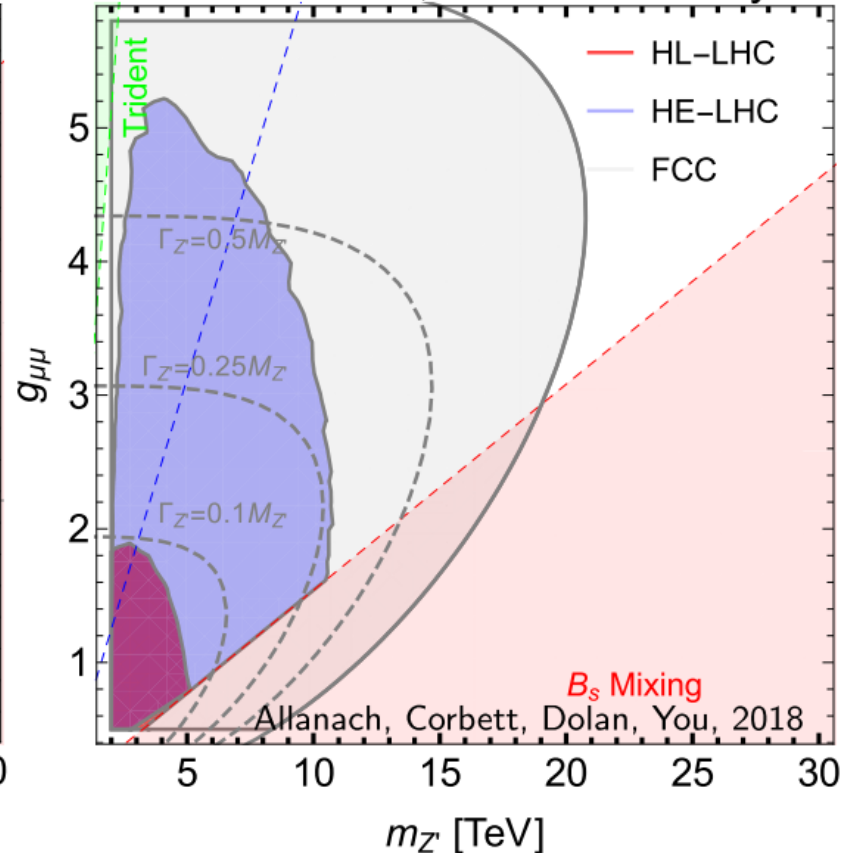
- Improved MC study including **large widths**:

MUM Model, 95% Sensitivity



Still a gap in coverage at low masses!

MDM Model, 95% Sensitivity



Take-Home Message: Z' sensitivity

- Drell-Yan, $p p \rightarrow Z' \rightarrow \mu^+ \mu^-$ for two flavour assumptions:
 - **Mixed-Up Model:**
 - HL-LHC: *No sensitivity*
 - HE-LHC: $M_{Z'}$, up to 13 TeV, width up to 30%
 - FCC-hh: $M_{Z'}$, up to 22 TeV, width up to 30%
 - **Mixed-Down Model:**
 - HL-LHC: $M_{Z'}$, up to 5 TeV, width up to 10%
 - HE-LHC: $M_{Z'}$, up to 10 TeV, width up to 60%
 - FCC-hh: $M_{Z'}$, up to 20 TeV (*entire parameter space*)

Take-Home Message: LQ sensitivity

- Pair production, $p p \rightarrow LQ LQ \rightarrow \mu^+ \mu^- j j$



- Single production, $p p \rightarrow LQ \rightarrow \mu^+ \mu^- j$

